

TD n°1 : PUISSANCE D'UN NOMBRE (Niveau 4^{ème})

Exercice 1:

Simplifier les écritures suivantes:

$6x \times 3x \times x = \dots\dots\dots$	$x^2 \times x \times x^3 = \dots\dots\dots$	$2x^2 \times 6x^5 = \dots\dots\dots$
$(x^3)^2 \times x \times (x)^3 = \dots\dots\dots$	$5a^3 \times 2a \times 4 = \dots\dots\dots$	$(-a)^2 a^3 = \dots\dots\dots$

Exercice 2: Remplacer chaque pointillé par l'entier naturel qui convient:

$$3^5 = 3^2 \times 3^{\dots}$$

$$2,5^{\dots} \times 2,5^3 = 2,5^7$$

$$0,4^{\dots} \times 0,4 = 0,4^2$$

$$a \times a^n \times a^{\dots} = a^{n+3}$$

$$(-3)^5 \times (-3)^{\dots} = (-3)^{-2}$$

$$(-0,5)^{\dots} \times (-0,5)^2 \times (-0,5)^{-7} = (-0,5)^{-1}$$

Remarque :

$$(-2)^2 = 2^2 = 4$$

$$(-2)^3 = -2^3 = -8$$

$$(-2)^4 = 2^4 = 16$$

$$(-2)^5 = -2^5 = -32$$

$$(-2)^6 = 2^6 = 64$$

car tout dépend de la parité de l'exposant, en effet par exemple :

$$(-2)^3 = (-2) \times (-2) \times (-2) = -8 \quad (\text{il y a 3 signes } -)$$

$$(-2)^4 = (-2) \times (-2) \times (-2) \times (-2) = +16 \quad (\text{il y en a 4})$$

Exercice 3:

Ecrire sous la forme d'une seule puissance:

$$A = 3^2 \times 5^2 = \dots\dots\dots$$

$$B = 3 \times 3^4 \times 3^7 = \dots\dots\dots$$

$$C = (-3) \times (-3)^4 = \dots\dots\dots$$

$$D = (-3)^{-3} \times (-3)^4 \times (-3)^3 = \dots\dots\dots$$

$$E = (-3)^2 \times 4^2 = \dots\dots\dots$$

$$F = 6^4 \times (-7)^4 = \dots\dots\dots$$

$$G = (3^7)^3 = \dots\dots\dots$$

$$H = (2^4)^3 \times 2^5 = \dots\dots\dots$$

$$I = (5^2)^4 \times 5 = \dots\dots\dots$$

$$J = 10^2 \times 10^{-5} \times 10^7 = \dots\dots\dots$$

$$K = \frac{10^2 \times 10^{-5} \times 10^7}{10^4 \times 10^2} = \frac{\dots\dots\dots}{\dots\dots\dots} = \dots\dots\dots$$

$$L = (10^2)^2 \times (10^{-5})^3 \times 10^7 = \dots\dots\dots$$

$$M = \frac{(10^2)^3 \times (10^{-5})^3 \times 10^2}{10 \times 10^{-3}} = \frac{\dots\dots\dots}{\dots\dots\dots} = \dots\dots\dots$$

Réponses

$A = 15^2$; $B = 3^{12}$; $C = -3^5$; $D = 3^4$; $E = +12^2$; $F = +42^4$; $G = 3^{21}$; $H = 2^{17}$; $I = 5^9$; $J = 10^4$
 $K = 10^{-2}$; $L = 10^{-4}$; $M = 10^{-5}$